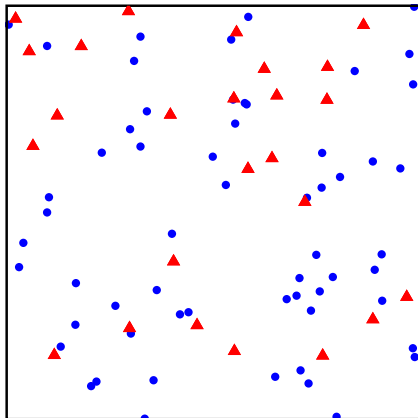


- 3 Mathematics and general framework
 - Our problem
 - Covers
 - Reformulation of the problem
 - Column generation
 - Pricing subproblem
 - Matheuristics

Our current problem

α -CMLP

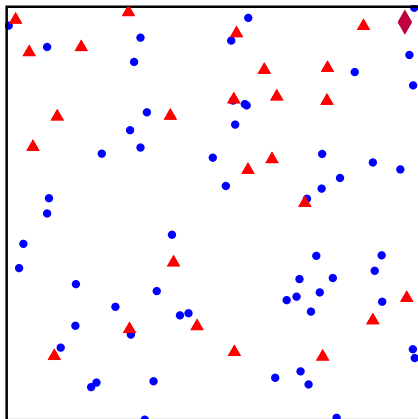
- set of targets and sensors



Our current problem

α -CMLP

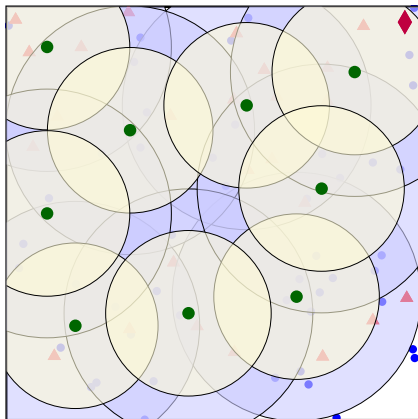
- set of targets and sensors
- base station



Our current problem

α -CMLP

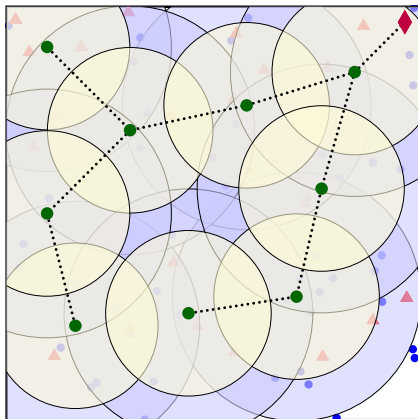
- set of targets and sensors
- base station
- activated sensors



Our current problem

α -CMLP

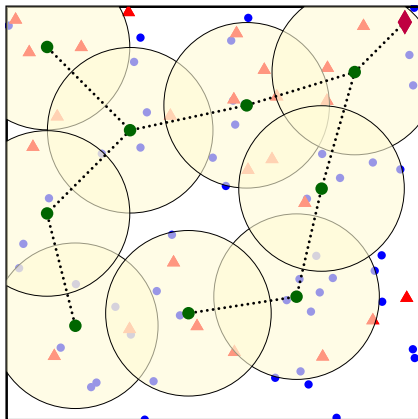
- set of targets and sensors
- base station
- activated sensors
- communication links



Our current problem

α -CMLP

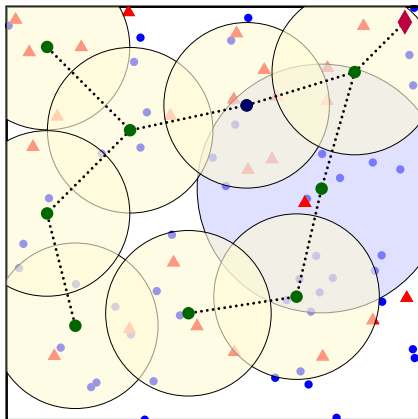
- set of targets and sensors
- base station
- activated sensors
- communication links
- α -coverage



Our current problem

α -CMLP-MR

- set of targets and sensors
- base station
- activated sensors
- communication links
- α -coverage
- some sensors can be used for communication only!

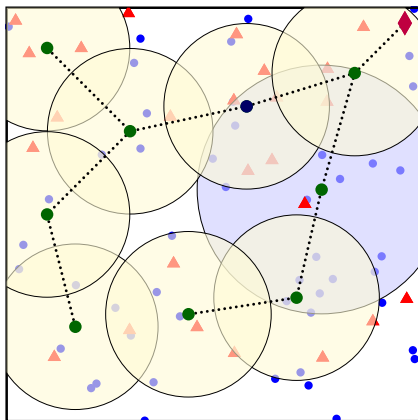


Our current problem

α -CMLP-MR

- set of targets and sensors
- base station
- activated sensors
- communication links
- α -coverage
- some sensors can be used for communication only!

We are now looking for subsets of active sensors and their role

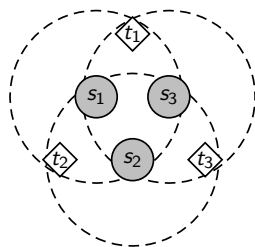


Definition (Cover)

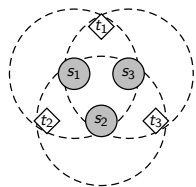
A **cover** is a subset of sensors used at the same time for covering a subset of targets

Examples:

- cover $\{s_1\}$ covers t_1 and t_2
- cover $\{s_1, s_2\}$ covers all the targets
- cover $\{s_1, s_3\}$ also covers all the targets

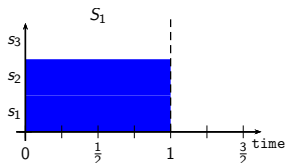
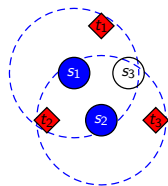


Scheduling the covers (disjoint covers)



In that small example, we have 3 covers $S_1 = \{s_1, s_2\}$, $S_2 = \{s_1, s_3\}$ and $S_3 = \{s_2, s_3\}$ that cover all the targets

Continuous use of covers (disjoint covers)

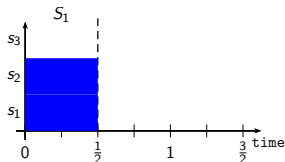
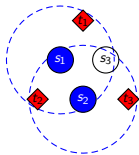


Battery depleted for s_1 and s_2 , other covers cannot be used.

If we want to cover **all the targets** with disjoint covers, maximum network lifetime is equal to 1

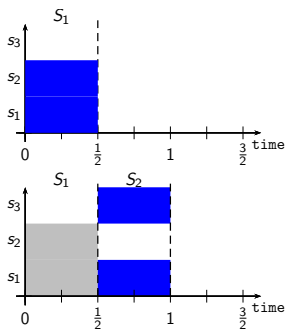
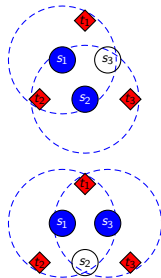
Scheduling the covers (non-disjoint covers)

Sequentially use $\{s_1, s_2\}$, $\{s_1, s_3\}$ and $\{s_2, s_3\}$ for 0.5 units of time each



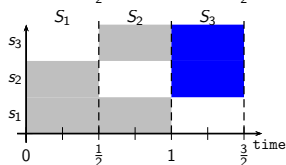
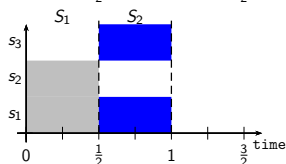
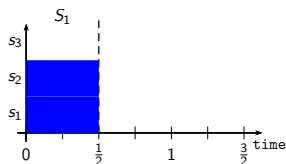
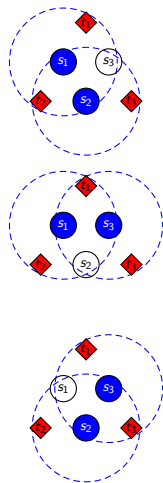
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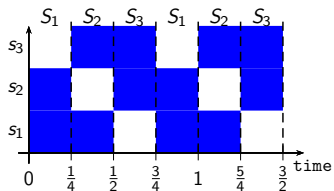
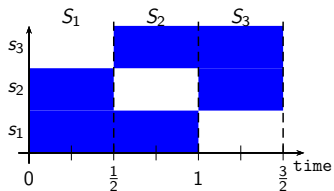
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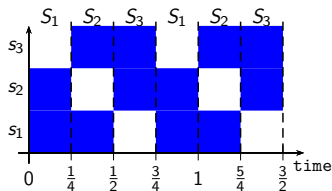
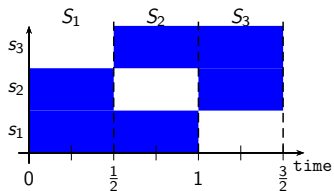
Scheduling the covers

Different schedules can conduct to equivalent solutions



Scheduling the covers

Different schedules can conduct to equivalent solutions



Questions:

- How can we find these covers?
- How long are we going to use them?

A very simple model

If we know how to build the covers, α -CMLP-MR is simply formulated by:

General LP model

$$\text{Maximize: } \sum_{j|C_j \in \Omega} t_j$$

$$\sum_{j|C_j \in \Omega} (E_{s_v}) t_j \leq \beta_{s_v} \quad \forall s_v \in S$$

$$t_j \geq 0 \quad \forall j|C_j \in \Omega$$

A simple model, but...

Remarks:

- Too many columns
15 sensors \approx 14 million columns



A simple model, but...

Remarks:

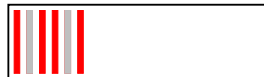
- Too many columns
15 sensors \approx 14 million columns
- Few columns are useful
15 sensors: at most 15 columns



A simple model, but...

Remarks:

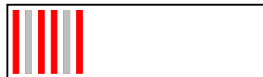
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- Strategy: generate them on the fly



A simple model, but...

Remarks:

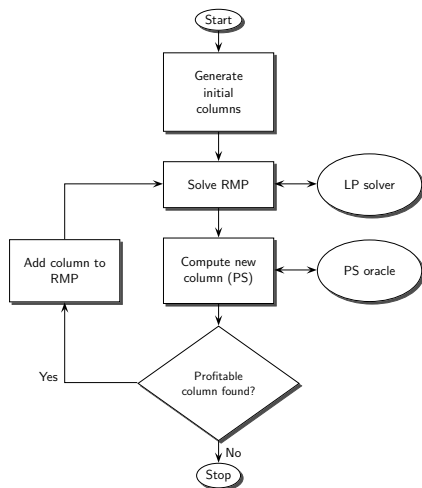
- Too many columns
15 sensors \approx 14 million columns
- Few columns are useful
15 sensors: at most 15 columns
- Strategy: generate them on the fly



Solution approach

Column generation is a natural approach to solve the problem

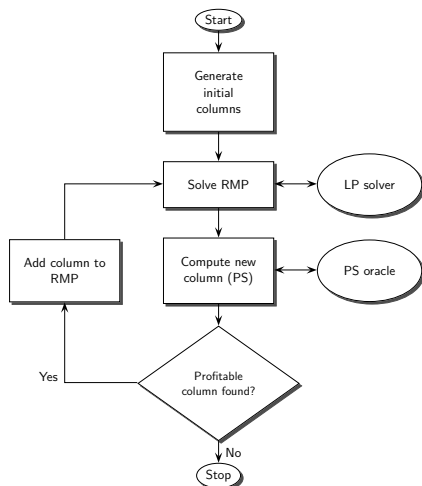
Principle of column generation approaches (CG)



Master Problem (RMP)

Maximizes network lifetime for the **available set of columns**

Principle of column generation approaches (CG)



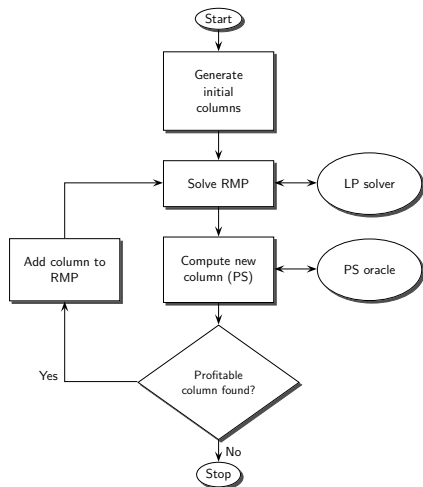
Master Problem (RMP)

Maximizes network lifetime for the **available set of columns**

Pricing Subproblem (PS)

Identifies **new** columns that can help to extend lifetime

Principle of column generation approaches (CG)



Master Problem (RMP)

Maximizes network lifetime for the **available set of columns**

Pricing Subproblem (PS)

Identifies **new** columns that can help to extend lifetime

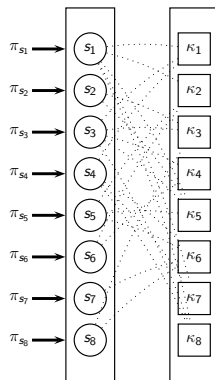
Performance might be poor...

- PS implementation issues
- Heading-in effect
- Tail-off effect

Solving the pricing subproblem

Data

- π_{s_i} : Dual variable value associated to battery constraint for sensor s_i



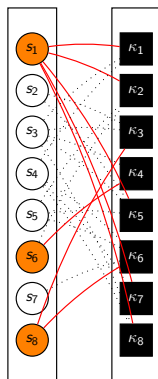
Solving the pricing subproblem

Decision variables

- sensor activity
 - $y_{s_i} \in \{0, 1\}$

Objective

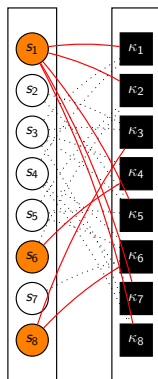
- Min: $\sum_{s_i \in \mathcal{S}} y_{s_i} \pi_{s_i}$
- Identify a subset of sensors with interesting reduced cost



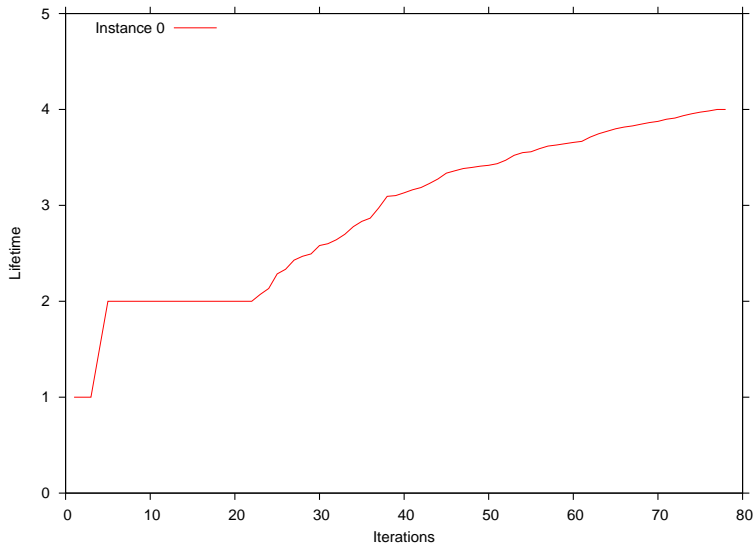
Solving the pricing subproblem

Remarks

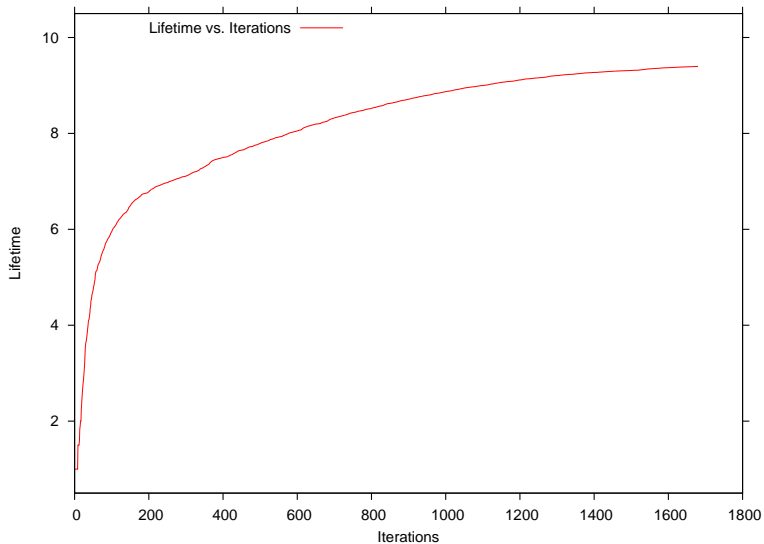
- Weighted set covering
NP-Hard
- One column per iteration
- Approximations lead to premature convergence



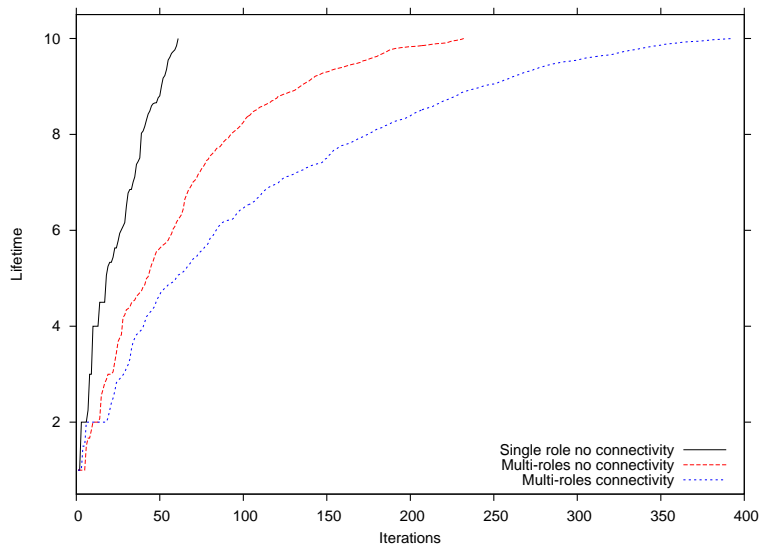
Heading-in effect



Tail-off effect



Tail-off effect

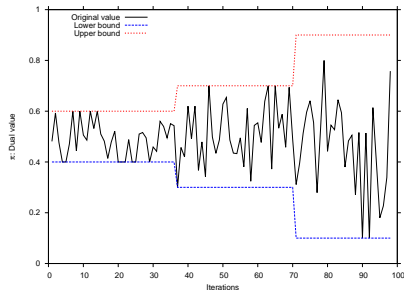


Classical stabilization strategies are explored

Stabilized CG

Manage dual variables:

- Dual variable stabilization
- Dual variable smoothing

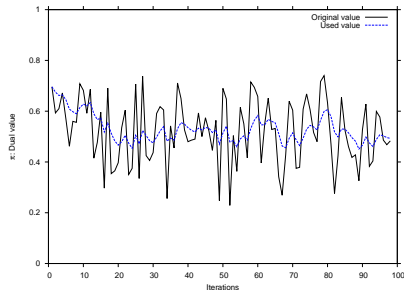


Classical stabilization strategies are explored

Stabilized CG

Manage dual variables:

- Dual variable stabilization
- **Dual variable smoothing**

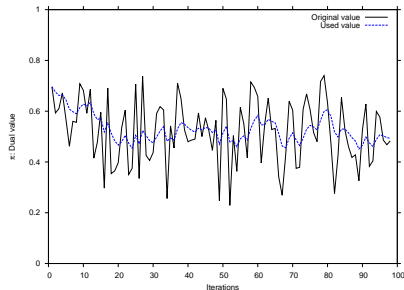


Classical stabilization strategies are explored

Stabilized CG

Manage dual variables:

- Dual variable stabilization
- Dual variable smoothing



Nice, but not very efficient. . .

Metaheuristics are used to intensify/diversify the search

Intensification

- GRASP
- VNS



Improvements – Intensification & diversification

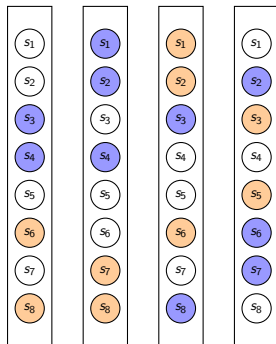
Metaheuristics are used to intensify/diversify the search

Intensification

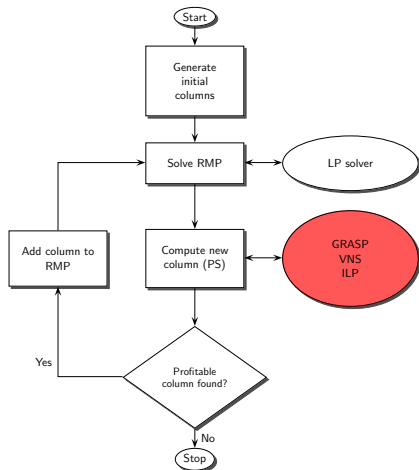
- GRASP
- VNS
- Evolutionary algorithms

Diversification

- Return multiple profitable columns



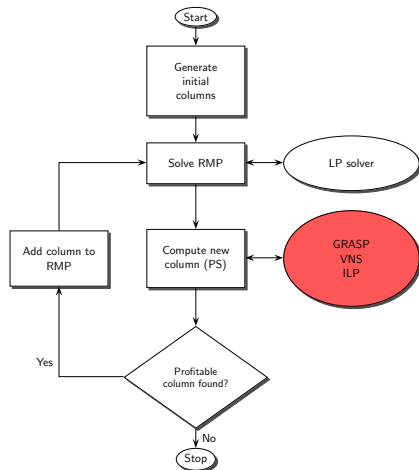
A new matheuristic framework



GRASP

Set covering with relaxed connectivity constraints + repair

A new matheuristic framework



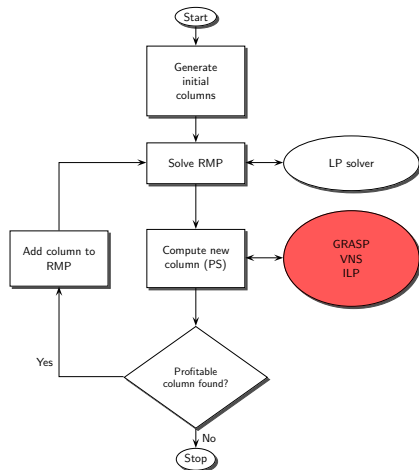
GRASP

Set covering with relaxed connectivity constraints + repair

VNS

Considering connectivity and coverage constraints

A new matheuristic framework



GRASP

Set covering with relaxed connectivity constraints + repair

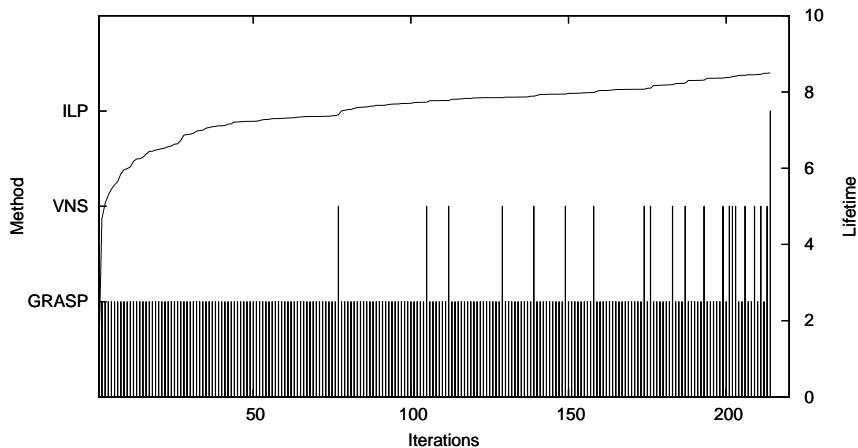
VNS

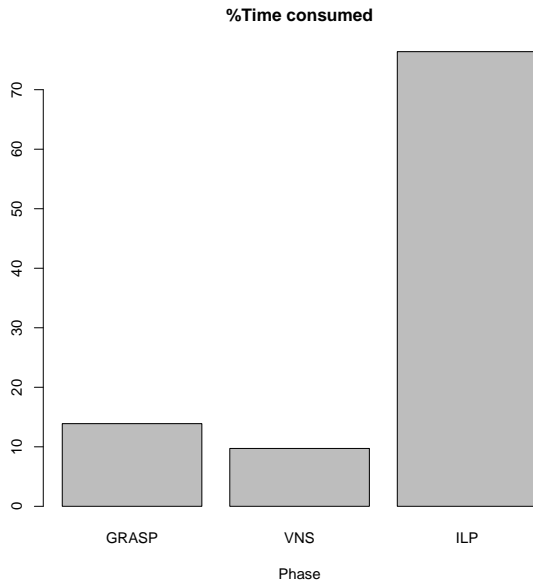
Considering connectivity and coverage constraints

ILP solver

Used to check optimality or discover difficult columns

Results





Techniques used for the pricing subproblem

- Evolutionary algorithm – find quickly several columns
- Constraint Programming – prove optimality
use specific tree variables and propagation

Other techniques and variants

Techniques used for the pricing subproblem

- Evolutionary algorithm – find quickly several columns
- Constraint Programming – prove optimality
use specific tree variables and propagation

Variants of the problem

- Multiple base stations
- Irregular shapes
- Directional sensors
- Obstacles
- Area coverage



A. Rossi, A. Singh, and M. Sevaux.

Column generation algorithm for sensor coverage scheduling under bandwidth constraints.
Networks, 60(3):141–154, 2012.



A. Rossi, A. Singh, and M. Sevaux.

An exact approach for maximizing the lifetime of sensor networks with adjustable sensing ranges.
Computers and Operations Research, 39(12):3166–3176, 2012.



A. Rossi, A. Singh, and M. Sevaux.

Lifetime maximization in wireless directional sensor network.
European Journal of Operational Research, 231(1):229–241, 2013.



A. Singh, A. Rossi, and M. Sevaux.

Matheuristic approaches for Q-coverage problem versions in wireless sensor networks.
Engineering Optimization, 45(5):609–626, 2013.



F. Castaño, A. Rossi, M. Sevaux, and N. Velasco.

A column generation approach to extend lifetime in wireless sensor networks with coverage and connectivity constraints.
Computers and Operations Research, 52(B):220–230, 2014.



F. Castaño, E. Bourreau, N. Velasco, A. Rossi, and M. Sevaux.

Exact approaches for lifetime maximization in connectivity constrained wireless multi-role sensor networks.
European Journal of Operational Research, 241(1):28–38, 2015.



M. Sevaux, M. Vecchio, and A. Bounceur, editors.

Special issue on Algorithms for Wireless Sensor Networks, volume x of *Algorithms*.
MDPI, 2015. Available online.



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Two important references



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MDPI, 2015. Available online.

- 4 Simulation and Demo
 - www.cupcarbon.com
 - a simulation tool
 - open source
 - java-based platform



www.cupcarbon.org

Launch the demo movie, if it works!!!

- 5 Conclusion & perspectives
 - On our work
 - Future trends

Our matheuristic framework

- is well suited for WSN lifetime maximization
- can adapt to many variants
- is fully customisable

And after...

- combination of all variants?
- moving targets (\rightarrow target tracking)
- moving sensors
- full integration in cup-carbon

And now, what's next?

UAV for professionals and for all



And now, what's next?

UAV for professionals and for all



And now, what's next?

UAV for professionals and for all

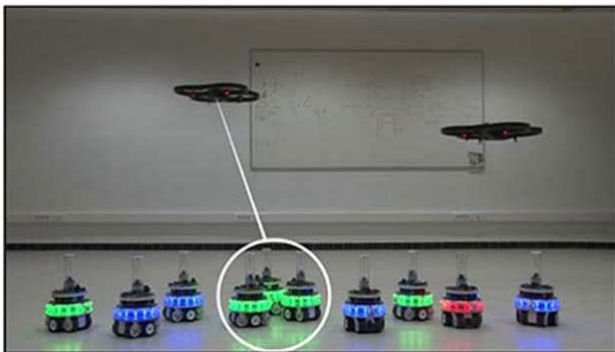


And now, what's next?

UAV for professionals and for all



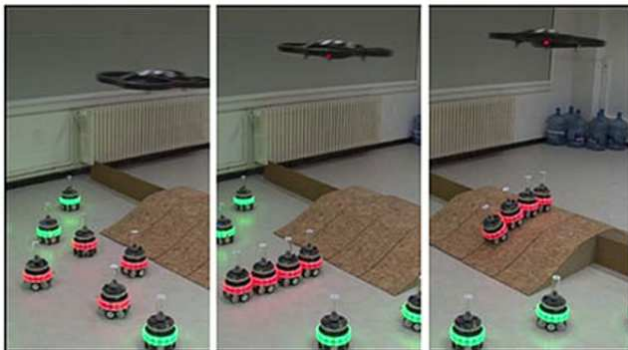
Cooperation among robots and UAV



And now, what's next?

UAV for professionals and for all

Cooperation among robots and UAV



And now, what's next?

UAV for professionals and for all



Cooperation among robots and UAV



UAV Swarms



And now, what's next?

UAV for professionals and for all



Cooperation among robots and UAV



UAV Swarms



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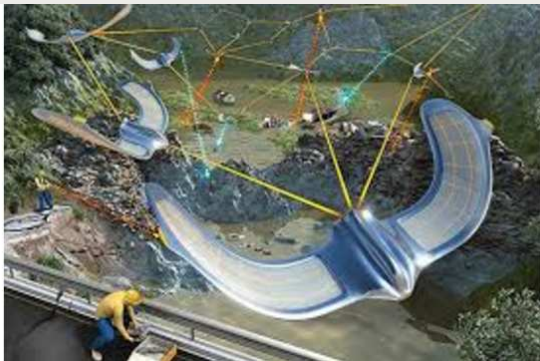
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UAV Swarms



Are we aware?¹

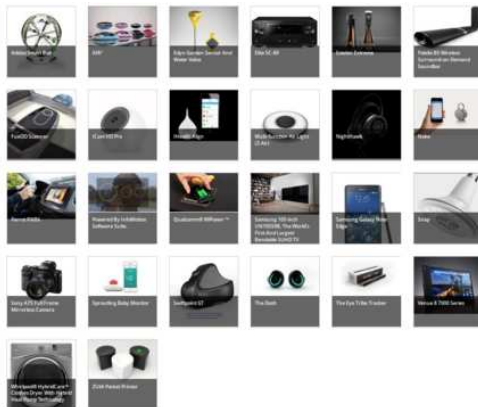


THE GLOBAL STAGE FOR INNOVATION

¹Quote from a famous Belgian actor!

Are we aware?¹

Among the 19 categories for innovation, 10 are related to sensors, wireless sensors or wireless sensor networks. . .



¹Quote from a famous Belgian actor!

Wireless Sensor Networks

A survey on maximizing lifetime in sensor coverage problems

Marc Sevaux

ORBEL 29

Université de Bretagne-Sud

www.univ-ubs.fr/or/

February 5, 2015

**JE SUIS
CHARLIE**

**IK BEN
CHARLIE**

